Different Speed Control Techniques of DC Motor: A Comparative Analysis
Virendra Singh Solanki, Virendra Jain, Anil Kumar Chaudhary
Department of Electrical and Electronics Engineering, RGPV university, Mandsaur, India
Virendra.s.solanki@gmail.com, er.virendrajain@gmail.com,
anilkumar6352@gmail.com

Abstract- The important control characteristics of DC motor have contributed in the extensive use of DC motor in the industry. With the increasing use of power semiconductor units, the speed control of DC motor is increasingly getting sophisticated and precise. Speed of the DC motor is controlled by controlling the armature voltage. Armature voltage is controlled using different single phase AC/DC converter. Half converter, semi converter, full converter and dual converter are some of the thyristor based circuits which are used for speed control of DC motor. This paper studies different speed control techniques of DC motor and makes a comparative study of different converter based speed controller techniques.

Index Terms- AC/DC converter, DC motor, speed control.

I. INTRODUCTION

DC motors are widely used in industry because of its low cost, less complex control structure and wide range of speed and torque. There are many methods of speed control of DC drives namely field control, armature voltage control and armature resistance control methods [2]. DC motors provide high starting torque which is required for traction applications. In DC motor control over a large speed range, both below and above the rated speed can be achieved quite easily. DC motors have inherent disadvantages that it needs regular maintenance and it is bulky in size. DC motors are tailor made, so it is very difficult to replace them. In general, armature voltage control method is widely used to control the DC drives. In this method, a controlled rectifier, or chopper is used but due to involvement of power electronics elements, nonlinear torque speed characteristics are observed which are undesirable for control performance [1].

Nowadays state of art speed control techniques of DC motor are available. Thyristor based DC drives with analog and digital feedback control schemes are used. Phase locked loop control technique is also used for precise speed control and zero speed regulation. In past, many researchers presented various new converter topologies of DC motor control for different applications of industry [5,6,8,9], but at the basic level in all of them thyristor based AC-DC converter are used. MATLAB with its toolboxes like Simulink and SimPowerSystem are used for simulation [3,7].

This paper provides a comparative study of different thyristor based speed control techniques.

II. MATHEMATICAL MODELLING OF DC MOTOR

The dynamic and steady-state model of separately excited DC motor is needed to analyse the torque speed characteristics. The schematic representation of the model of a separately excited DC motor is shown below in figure 1 in which $e_a$ is the terminal voltage applied to the motor, $R_a$ and $L_a$ are the resistance, and inductance of the armature circuit respectively, $R_f$ and $L_f$ are the resistance, and inductance of the field circuit respectively, $e_b$ is generated back emf and $T_m$ is the electromagnetic torque developed by the motor. The related DC Motor parameters are mentioned in appendix A.

![Figure 1: Equivalent circuit of separately excited DC motor](image)

The torque is produced as a result of interaction of field flux with current in armature conductors and is given by Eq. (1)

$$T_m = K_f i_a$$  \hspace{1cm} (1)

Here $T_m$ is a constant depending on motor windings and geometry and $i_a$ is the flux per pole due to the field winding.

The direction of the torque produced depends on the direction of armature current. When armature rotates, the flux linking the armature winding will vary with time and therefore according to Faraday’s law, an emf will be induced across the winding. This generated emf, known as the back emf, depends on speed of rotation as well as on the flux produced by the field and given by Eq. (2)

$$e_b = K_f \phi$$  \hspace{1cm} (2)

By applying KVL at input side of in figure 1,

$$e_a = i_a R_a + L_a \frac{di_a}{dt} + e_b$$  \hspace{1cm} (3)

In steady state condition, $E_a = I_a R_a + E_b$
In terms of torque and speed, the steady state equation will be given by Eq. (5)

$$E_u = \frac{T_m}{K_f} R_a + K_f \omega \phi$$

(5)

So, \( \omega = \frac{E_u}{K_f} - \frac{T_m}{(K_f R_a)^2} R_a \)

(6)

Thus from the above equation it is clear that speed can be controlled by varying there parameters, namely , , and . The three methods of speed control are as following:

i. Armature voltage controlled ( ).
ii. Armature resistance controlled ( ).
iii. Flux controlled ( ).

Speed control using armature resistance by adding external resistor is not used very widely because of the large energy losses due to the \( R_{esr} \). Armature voltage control is normally used for speed up to rated speed (base speed). Flux control is used for speed beyond rated speed but at the same time the maximum torque capability of the motor is reduced since for a given maximum armature current, the flux is less than the rated value and so as the maximum torque produced is less than the maximum rated torque [4]. Here the main attention is given to the armature voltage control method. In the armature voltage control method, the voltage applied across the armature \( e_a \) is varied keeping field voltage constant. As equation (6) indicates, the torque-speed characteristic is represented by a straight line with a negative field voltage constant. As equation (6) indicates, the ideal torque-speed characteristic is illustrated in figure 2 [10].

![Figure 2: Torque speed characteristics of the separately excited DC motor at different armature voltages](image)

III. THYRISTOR BASED TECHNIQUES OF DC MOTOR SPEED CONTROL

A half wave converter in the field circuit will increase the

A separately excited DC motor fed through single phase half wave converter is shown in figure 3. Single phase half wave converter feeding a DC motor offers only one quadrant drive. Such type of drives are used up to about 0.5 kW DC motor.

![Figure 3: Single phase half wave converter drive](image)

For single phase half wave converter, average output voltage of converter can be calculated as, given as Eq. (7)

$$V_m \approx V_0 = \frac{V}{2\pi} (1 + \cos \alpha), \text{ for } 0 < \alpha < \pi$$

(7)

magnetic losses of the motor due to high ripple content on the field excitation current, so an ideal DC source is preferred over half wave converter for field circuit. A separately excited DC motor fed through single phase semiconverter is shown in figure 4. This converter also offer only one quadrant drive and is used up to 15 kW DC drives.

![Figure 4: Single phase semi converter drive](image)

With a single phase semiconverter in the armature circuit, equation (8) gives the average armature voltage as,

$$V_0 = V_i = \frac{V_m}{\pi} (1 + \cos \alpha), \text{ for } 0 < \alpha < \pi$$

(8)
The armature voltage is varied by single phase full wave converter as shown in figure 5. It is a two quadrant drive, and is limited to applications up to 15kW. The armature converter gives \(+V_o\) or \(-V_o\) and allows operation in the first and fourth quadrant. The converter in the field circuit could be semi, full or even dual converter. The reversal of the armature or field voltage allows operation in the second and third quadrant.

![Figure 5: Single phase full converter drive](image)

The average armature voltage in armature circuit for single phase full converter drive is given by Eq. (9)

\[
V_o = V_f = \frac{2V_m}{\pi} (1 + \cos \alpha), \text{ for } 0 < \alpha < \pi
\]

(9)

To realize single phase dual converter, two single phase full converters are connected as shown in figure 6.

![Figure 6: Single phase dual converter drive](image)

In fig. 6, there are two single phase full wave converters either converter 1 operates to supply a positive armature voltage \(V_o\), or converter 2 operates to supply negative armature voltage \(-V_o\). Converter 1 provides operation in first and fourth quadrants, and converter 2 provides operation in second and third quadrants. It is four quadrant drive and provides four modes of operation: forward powering, forward braking (regeneration), reverse powering, and reverse breaking (regeneration). The field converter could be a full wave converter, a semiconverter, or a dual converter.

If converter 1 operates at a firing angle of \(\alpha_f\) then equation (10) gives the armature voltage as,

\[
V_o = V_f = \frac{V_m}{\pi} (1 + \cos \alpha_f), \text{ for } 0 < \alpha_f < \pi
\]

(10)

And similarly, if converter 2 operates at a firing angle of \(\alpha_f\) then equation (11) gives the armature voltage as, [11].

\[
V_o = V_f = \frac{V_m}{\pi} (1 + \cos \alpha_f)
\]

(11)

IV. SIMULATION

To investigate the effect of armature voltage on the torque speed curve six different firing angles are used with the voltage applied to the field circuit kept constant 300V. A constant 240 V, 50 Hz AC supply is applied to the input of single phase half wave converter. The average value of converter output is controlled by changing the firing angle \(\alpha\).

A cosine firing angle scheme is used to change the firing angle. The firing angles used to get different output voltages for armature are 0°, 18°, 36°, 54°, 72° and 89°.

The simulink model used to get torque speed characteristic for a single phase half wave converter is shown in figure 7.

![Figure 7: Simulink realization of armature voltage speed control method using a single phase half wave converter drive](image)

The torque speed curves for a single phase half wave converter drive are shown in figure 8.
It is clear that torque speed contains both linear and non linear regions. The linear region of operation for 0° firing angle approximately starts at 100 N.m load torque, but for 18° firing angle linear region starts at 105 N.m load torque, while for 36° firing angle linear region starts at approximately at 110 N.m and so on. The discontinuous armature current results in a highly non-linear torque speed characteristic. Figure 9 and 10 shows the armature voltage and current obtained at 50 N.m (in the non-linear region) and 135 N.m (in linear region) with firing angle 89°. These figures clearly show the discontinuous and continuous operation of single phase half wave converter drive in non linear and linear regions, respectively.

To investigate the effect of armature voltage on the torque speed characteristic, six different firing angles are applied to the firing angle generator while the voltage applied to the field circuit is kept constant 300V. A constant 240V, 50Hz AC is applied to the input of single phase semi converter. The average value of the converter output is controlled by the firing angle (α). The firing angles used to get different output voltages for armature are 0°, 18°, 36°, 54°, 72° and 89°. The simulink model used to get torque speed characteristic for a single phase half wave converter is shown in figure 11.

The fig 12, showing the torque speed characteristics, the non linear and linear operating regions are clearly visible for different firing angles. The linear operating range for single phase semi converter drive decrease as firing angle increases. For firing angle 0°, it is 60 to 180 N.m, for 18° it is 65 to 180 N.m, for 36° it is 80 to 180 N.m and for 89° it is 100 to 180 N.m. The non linearity in the speed torque characteristic is due to the discontinuity in armature current. Figure 13 and 14 shows the armature voltage and current obtained at 50 N.m (in the non-linear region) and 135 N.m (in linear region) with firing angle 0°. These figures show the discontinuous and continuous operation of single phase semiconverter drive in non linear and linear regions, respectively.
Figure 13: Armature current and voltage at 50N.m with firing angle 0° for single phase semiconverter drive

Figure 14: Armature current and voltage at 135N.m with firing angle 0° for single phase semiconverter drive

The simulink model used to get torque speed characteristic for a single phase full converter drive is shown in figure 15. The effect of armature voltages on the torque speed characteristic is observed for six different firing angles, as the voltage applied to the field circuit is kept constant at 300V, and a constant 240V, 50 Hz AC is applied to input of single phase full converter. The average value of applied armature voltage is varied by varying the firing angle of full converter.

Figure 15: Simulink realization of armature voltage speed control method using a single phase full converter drive

Figure 16: Torque-speed characteristics for a single phase full converter drive

Linear and non linear regions for single phase full converter drive are clearly visible in the above shown torque speed curve. Non linearity is because of the discontinuity in the armature current, and also it is observed that the range of non linearity increases as firing angle is increased. For firing angle 0°, non linearity range of load torque 0 to 85 N.m, for 18° it is 0 to 100 N.m, for 36°, it is 0 to 110 N.m., for 54° it is 0 to 54 N.m and for 89° it is 0 to 120 N.m. The armature voltage and current waveforms for single phase full converter drives are shown in figure 17 and 18. These were obtained at 50 N.m (in the non-linear region) and 135 N.m (in linear region) with firing angle 89°. These figures show the discontinuous and continuous operation of single phase full converter drive in non linear and linear regions, respectively.

Figure 17: Armature current and voltage at 50N.m with firing angle 89° for single phase full converter drive
The parameters of separately excited DC motor

<table>
<thead>
<tr>
<th></th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated Power (P)</td>
<td>5 Hp</td>
</tr>
<tr>
<td>Rated Armature Voltage</td>
<td>240 V</td>
</tr>
<tr>
<td>Armature Resistance (R_a)</td>
<td>2.518 (\Omega)</td>
</tr>
<tr>
<td>Armature Inductance (L_a)</td>
<td>0.028 H</td>
</tr>
<tr>
<td>Field Resistance (R_f)</td>
<td>281.3 (\Omega)</td>
</tr>
<tr>
<td>Field Inductance (L_f)</td>
<td>156 H</td>
</tr>
<tr>
<td>Rated Speed</td>
<td>1750 RPM</td>
</tr>
<tr>
<td>Rated Field Voltage</td>
<td>300 V</td>
</tr>
</tbody>
</table>

### V. Conclusion

This paper presents speed control of separately excited DC motor using different single phase AC/DC converter. Speed torque curves for three types of single phase AC/DC converter (Half wave converter, Semiconverter and full converter) are obtained for a wide-range of loading conditions. From the above results, it can be concluded that the reason of non linearity in speed torque curve is discontinuity in armature current which is highly non-desirable for industrial applications. To remove the discontinuity in armature current an inductor should be used in series to make the armature current continuous. It is also observed that the range of non linearity is small in semiconverter as compared to half wave and full converter drives, so semi converter drives can be preferred for the wide range of load torque.

### Table I: Linear operating range of Load torque for different converter drives and firing angles

<table>
<thead>
<tr>
<th>Drive type</th>
<th>Firing angle</th>
<th>Half wave Drive</th>
<th>Semiconverter Drive</th>
<th>Full wave converter Drive</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
<td>100 to 180</td>
<td>60 to 180</td>
<td>85 to 180</td>
</tr>
<tr>
<td></td>
<td>18</td>
<td>105 to 180</td>
<td>65 to 180</td>
<td>100 to 180</td>
</tr>
<tr>
<td></td>
<td>36</td>
<td>110 to 180</td>
<td>80 to 180</td>
<td>110 to 180</td>
</tr>
<tr>
<td></td>
<td>54</td>
<td>115 to 180</td>
<td>100 to 180</td>
<td>145 to 180</td>
</tr>
<tr>
<td></td>
<td>72</td>
<td>120 to 180</td>
<td>80 to 180</td>
<td>120 to 180</td>
</tr>
<tr>
<td></td>
<td>89</td>
<td>130 to 180</td>
<td>100 to 180</td>
<td>120 to 180</td>
</tr>
</tbody>
</table>

Figure 18: Armature current and voltage at 135N.m with firing angle 89° for single phase full converter drive

It is clearly seen that for all firing angle, the linear region of operation extends when single phase semi converter is used. The linear operating ranges of load torque for different converter drives with respect to firing angles are tabulated in table 1.
REFERENCES


AUTHORS

First Author – Virendra singh solanki ,is a, M.E.student ,MIT Mandsaur ,RGPV University, Mandsaur,MP, India-458001
E-mail ID: virendra.s.solanki@gmail.com

Second Author – Virendra Jain, is a, M.E.student ,of MIT Mandsaur ,RGPV University, Mandsaur,MP, India-458001
E-mail ID: e r v i r e n d r a @ g m a i l . c o m

Third Author – Anil Kumar Chaudhary, Assistant Professor in MIT Mandsaur, RGPV University,MP,458001
E-mail ID: anilkumar6352@gmail.com