

Empirical Modelling and Optimization of Zinc Chloride Activated Ngbo Clay Catalysts Using Response Surface Methodology

Veronica Nnenna Nwobasi¹, Francisca Ogechukwu Oshim^{2*} and Chinedu J. Nwali¹

¹Department of Chemical Engineering, Ebonyi State University, Nigeria

²School of Engineering, University of Greater Manchester, United Kingdom

DOI: <https://doi.org/10.51583/IJLTEMAS.2025.1410000141>

Received: 14 September 2025; Accepted: 22 September 2025; Published: 22 November 2025

Abstract: In this study, Box-Behnken's Response Surface Methodology (RSM) was applied to study the esterification reaction effectiveness of zinc chloride activated Ngbo clay catalyst. The XRF result showed that both raw and activated clay contain contaminations of oxides and other impurities; however, the clay mineral compositions are not significantly affected by zinc chloride treatments. Additionally, it indicates a high content of silicon and aluminium oxides compared to other oxides. XRD pattern results showed several characteristic peaks due to the mineral compositions present. The analysis of the peaks showed sharp peaks with low intensity at $2\theta = 11.300$, which corresponds to the main peak used in the identification of kaolinite clay, as reported in the literature. The esterification was monitored based on the process conditions of temperature, time duration, amount of reactant, catalyst weight and particle size. The Box -Behnken's Response Surface Methodology indicates that the zinc chloride clay-catalysed esterification reactions proceed through dual mechanisms: an Acid-complex and an Alcohol-complex mechanism, with the Alcohol mechanism dominating. The esterification efficiencies of acetic acid and ethanol by zinc chloride activated Ngbo clay catalyst, optimized using RSM models indicated the estimated esterification percentage of >95%. The predicted and experimental values obtained under the same conditions showed a difference of less than 5%, indicating that the Box-Behnken design approach is an efficient, effective, and reliable method for the esterification of acetic acid with ethanol. The produced catalyst was optimized using A-One way ANOVA modelling, which indicated a correlation coefficient of the regression of 0.9551, which implies that 95.51% of the total variation in the esterification reaction was attributed to the experimental variables. The result obtained indicated that the process could be applied in the esterification of acetic acid to avoid the drawbacks of corrosion, loss of catalyst and environmental problems.

Keywords: Optimization, Characterization, Esterification, Zinc Chloride Activated Clay Catalyst, Thermal activated catalyst, Response Surface Methodology, Box-Behnken design

I. Introduction

Clay is one of the abundant raw materials in Nigeria. It is readily available in Nigeria in large deposits, yet its potential has not been fully explored. However, there is recent interest in exploring the potentials of clays, such as in the bleaching of palm oil [1, 2], in the adsorption of dyes [3 – 5], among others. In a quest to develop green processes, clay is mostly used in the synthesis of catalysts, although the use of Nigerian clays from Ngbo, Ohaukwu, Ebonyi State, for producing clay catalysts is limited in the literature. Still, the kinetics of clay-catalysed esterification reaction is abundant in literature, but with little or no data on the mechanistic and empirical modelling on the use of Ngbo clay in this regard.

Esterification reactions have long been carried out in homogeneous phase in the presence of acid catalysts such as sulphuric acid, hydrochloric acid and p-toluene sulfonic acid (p-TSOH); which have drawbacks of corrosion, loss of catalyst and environmental problems [6, 7]. Therefore, researchers have been focused on developing eco-friendly heterogeneous catalysts for the synthesis of fatty acid esters. The most popular solid acid catalysts used to produce esters were ion-exchange organic resins, such as Amberlyst-15 [8, 9], Zeolites [10 – 11], [12] and Silica-supported heteropoly acid [13] and [14]. Nevertheless, they have shown limitations in applicability for catalysing esterification reaction due to low thermal stability (Amberlyst-15 <140 °C), mass transfer resistance (Zeolites) [15], [16], or loss of active acid sites in the presence of a polar medium (HPA/silica) [14].

A cost-benefit and environmental impact analysis of zinc chloride compared to alternative activation methods (thermal, acid, or alkaline treatment) would increase industrial relevance. Additionally, incorporating kinetic modelling could substantiate mechanistic claims more rigorously. Bench marking catalyst performance against established heterogeneous catalysts under identical conditions would also enhance the comparative value, supporting practical adoption in green chemical processes.

Response Surface Methodology (RSM) is a collection of statistical and mathematical techniques that uses quantitative data. Central composite design (CCD), Box-Behnken design (BBD), and Doehlert design are among the principal response surface methodologies used in experimental design. This method is suitable for fitting a quadratic surface, and it helps to optimize the effective parameters with a minimum number of experiments, and also to analyze the interaction between the parameters [9]. The objective is to optimize a response (output variable) which is influenced by several independent variables (input variables). The application of RSM to design optimization aims to reduce the cost of numerous expensive experiments, save time, and alleviate stress [17–20].

This work investigated the use of local clay from Ngbo in Ohaukwu Local Government Area of Ebonyi State, Nigeria for the production of zinc chloride activated catalyst and optimizes the effectiveness of the clay catalyst for the esterification of acetic acid with ethanol using Response Surface Methodology.

II. Materials and Methods

Source of Raw Materials

The clay sample was obtained from Ngbo in Ohaukwu L.G.A. of Ebonyi State (N 06°30' 32.8''), (E 007°58'13.7''). Chemicals used, such as Zinc Chloride (aq), NaOH, Acetic Acid, ethanol, distilled water, etc, were all of standard grade. They were purchased in a chemical shop at Ogbete main market Enugu, Enugu State.

Physico-Chemical Characterization of Ngbo Clay

The Ngbo clay sample was subjected to physical analysis to determine its physical properties. The analysis carried out includes: Bulk density, Moisture content, pH and Loss on Ignition (LOI).

Characterisation of the raw clay and Zinc chloride activated sample

The Ngbo clay sample was characterised using XRF and XRD.

Zinc Chloride Activation

The activation method used in this work is as reported by [21]. A 100g of pulverized and screened clay was mixed into a slurry with 50ml of diluted water, 30ml of 1M ZnCl₂ (aq) was added and stirred vigorously and placed in an oven where it was maintained at a temperature of 100°C. The sample was washed thereafter and left to sediment. Complete removal of all residual zinc chloride was achieved by repeating the washing and decanting process until a pH of 6 was obtained. The final slurry was filtered and dried at 100 °C. The dried, activated and washed clay was then pulverized, screened and stored in desiccators before use.

Optimization of Process Conditions on the Catalyst Quality Produced Using Esterification Process

Sample Preparation/Procedure

The raw clay sample was crushed and sieved at 100 microns, 200 microns, and 300 microns. Thereafter, the clay sample was activated using zinc chloride. The activated clay sample was used in an esterification reaction to assess the effectiveness. The Predetermined weight of the clay sample was weighed; one mole of Ethanol and acetic acid was each pipetted into the clay sample to ensure that the ethanol did not block the active sites of the catalyst. The container was tightly closed, the contents were shaken vigorously and immersed in a water bath shaker maintained at the conditions of the experimental design in Table 1. The summary of the reaction equation is:



On titration, the equation becomes:



Table 1: The natural and coded values of the independent variables used

VARIABLES	NATURAL VALUES			CODED VALUES		
	Low level	Mid-point	High level	Low level	Mid Point	High level
Temperature (°C), A	50	70	90	-1	0	+1
Process duration (minutes), B	30	195	360	-1	0	+1
Excess reactant (ml), C	2.5	3.75	5	-1	0	+1
Catalyst weight (grammes), D	0.25	0.38	0.5	-1	0	+1
Particle size (microns), E	100	200	300	-1	0	+1

The clay-catalysed esterification was modelled using Box-Behnken Response Surface Methodology.

For five factors inputs of x_1, x_2, x_3, x_4 and x_5 , the equation of the quadratic response is given as;

$$Y = b_0 + b_1X_1 + b_2X_2 + b_3X_3 + b_4X_4 + b_5X_5 + b_{12}X_1X_2 + b_{13}X_1X_3 + b_{14}X_1X_4 + b_{15}X_1X_5 + b_{23}X_2X_3 + b_{24}X_2X_4 + b_{25}X_2X_5 + b_{34}X_3X_4 + b_{35}X_3X_5 + b_{45}X_4X_5 + b_{11}X_1^2 + b_{22}X_2^2 + b_{33}X_3^2 + b_{44}X_4^2 + b_{55}X_5^2. \quad (3)$$

III. Response Surface Methodology

The response surface technique, applying a Box-Behnken design matrix, was used to study the interaction and effects among the factors and their level of contributions and significance in the clay-catalysed esterification. This method determines the optimal working conditions in a shorter timeframe, and provides detailed information on the conditions of the processes. This was achieved through a designed experimental design applying Box-Behnken Response Surface Methodology design of 46 steps of experiment consisting of five factors and three levels (Table 2). The numerical optimization method of RSM was used in the optimization.

Table 2: Box-Behnken’s Response Surface Methodology Design of Experiment

Std	Run	Factor A (°C)	Factor B (min)	Factor C (ml)	Factor D(g)	Factor E (mic)	Response (ml)	Yield (%)
37	1	70	30	3.75	0.25	200		
22	2	70	360	2.5	0.38	200		
23	3	70	30	5	0.38	200		
29	4	70	195	2.5	0.38	100		
26	5	90	195	3.75	0.25	200		
1	6	50	30	3.75	0.38	200		
32	7	70	195	5	0.38	300		
46	8	70	195	3.75	0.38	200		
10	9	70	360	3.75	0.38	100		
34	10	90	195	3.75	0.38	100		
21	11	70	30	2.5	0.38	200		
35	12	50	195	3.75	0.38	300		
8	13	70	195	5	0.5	200		
4	14	90	360	3.75	0.38	200		
2	15	90	30	3.75	0.38	200		
11	16	70	30	3.75	0.38	300		
31	17	70	195	2.5	0.38	300		
3	18	50	360	3.75	0.38	200		
24	19	70	360	5	0.38	200		
16	20	90	195	5	0.38	200		
44	21	70	195	3.75	0.38	200		
12	22	70	360	3.75	0.38	300		
36	23	90	195	3.75	0.38	300		
17	24	70	195	3.75	0.25	100		
18	25	70	195	3.75	0.5	100		
45	26	70	195	3.75	0.38	200		
33	27	50	195	3.75	0.38	100		
25	28	50	195	3.75	0.25	200		
20	29	70	195	3.75	0.5	300		
27	30	50	195	3.75	0.5	200		
30	31	70	195	5	0.38	100		

42	32	70	195	3.75	0.38	200		
41	33	70	195	3.75	0.38	200		
39	34	70	30	3.75	0.5	200		
6	35	70	195	5	0.25	200		
43	36	70	195	3.75	0.38	200		
38	37	70	360	3.75	0.25	200		
19	38	70	195	3.75	0.25	300		
40	39	70	360	3.75	0.5	200		
7	40	70	195	2.5	0.5	200		
28	41	90	195	3.75	0.5	200		
14	42	90	195	2.5	0.38	200		
5	43	70	195	2.5	0.25	200		
13	44	50	195	2.5	0.38	200		
9	45	70	30	3.75	0.38	100		
15	46	50	195	5	0.38	200		

IV. Results and Discussions

Physical properties of the raw clay

The physical properties of raw Ngbo clay are presented in Table 3. The result showed that the clay has a moisture content of 3.3 % and a bulk density of 1.25 g/ml, which are in agreement with the previous research of [22 – 24] that reported the moisture content of kaolinite clay is between 3.0 – 4.0% and the bulk density is 1.2 – 1.4 g/ml.

Table 3: Results of Bulk density, Moisture content, pH, and LOI

Clay type	Bulk density (g/ml)	% moisture content	pH	LOI (%)
Ngbo clay	1.25	3.33	7.5	10.52

Characterization of Raw Clay and Zinc Chloride Activated Clay

The chemical properties of the raw Ngbo clay were analysed using XRF and XRD.

The result of the XRF composition analysis of rawNgbo clay and Zinc Chlorideactivated Ngbo clays (ZAC) is presented in Table 4. The result showed that raw and activated clays have contaminations of oxides and other impurities, but the clay mineralcompositions are not meaningfully affected by zinc chloridetreatments even under strong conditionsand below 500 °C as reported in literature by [25, 26] and[27]. This indicates that improving the properties of the clay through chemical methods below 500 °C is challenging due to its low reactivity. This result of the XRF on the Ngbo raw clay and zinc chlorideactivated Ngbo clays, as shown in Table 4, also indicates high content of silicon and aluminium oxides compared to other oxides.

Table 4: Results of XRF analysis of raw Ngbo Clay and Zinc Chloride activated Ngbo clay

Chemical constituent	Raw clay (Wt. %)	Zinc Chloride activated (ZAC), (Wt. %)
SiO ₂	62.70	65.743
TiO ₂	1.52	1.386
Al ₂ O ₃	19.70	23.457
Fe ₂ O ₃	2.06	5.855
P ₂ O ₃	–	0.000

CaO	0.789	0.232
MgO	0.026	0.522
Na ₂ O	0.20	0.256
K ₂ O	0.85	1.149
Mn ₂ O ₃	–	0.135
V ₂ O ₅	0.071	–
Cr ₂ O ₃	0.035	0.011
CuO	0.044	–
BaO	0.19	–
L.O.I	11.82	–
SO ₃	–	0.181
Cl	–	0.131
ZnO	–	0.936
SrO	–	0.007

The results of XRD pattern analysis of raw Ngbo clay are presented in Figure 1. The XRD pattern results showed several characteristic peaks due to the mineral compositions present. The peak obtained at a position corresponding to $2\theta = 22.64^\circ$ indicated the presence of large quantities of quartz. Minor impurities, such as illite, muscovite, halloysite, quartz, hydrated mica, non-crystalline hydroxide iron and halloysite are present. The presence of these minor impurities and quartz content in Ngbo clay needs to be reduced to a minimum before its usage for industrial purposes, especially in catalysts development in line with the research of [28 and 29]. The XRD analysis corroborates the results obtained with the XRF analysis.

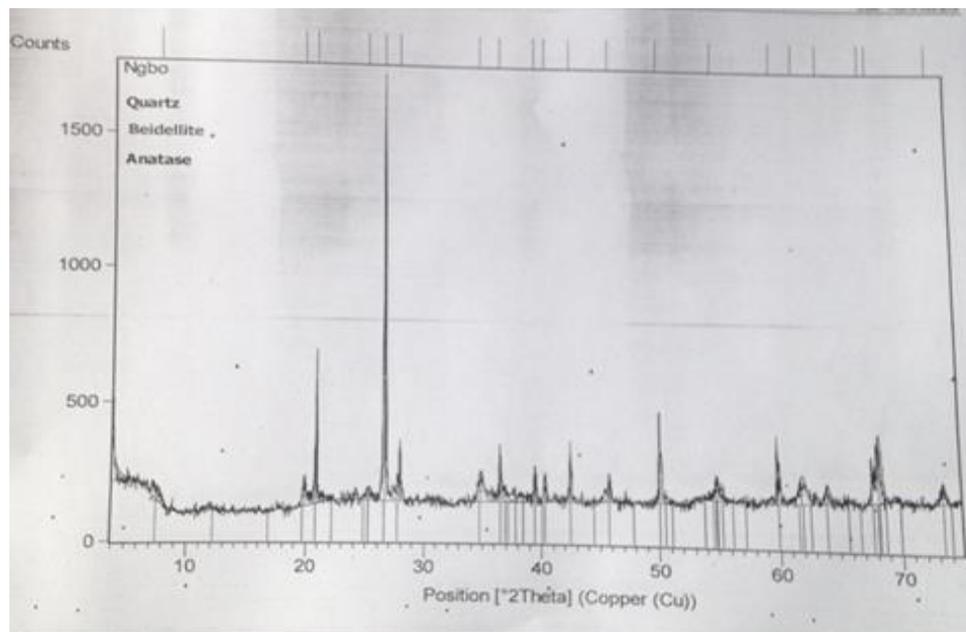


Figure 1: Results of XRD analysis of Ngbo raw clay

The results of XRD pattern analysis of Ngbozinc chloride activated catalyst, ZAC is presented in figure 2. The XRD pattern results showed several characteristic peaks due to the mineral compositions present. The analysis of the peaks showed sharp peaks with low intensity at $2\theta = 11.30^\circ$, which is the main peak used in the identification of kaolinite clay as reported in literature by [30].

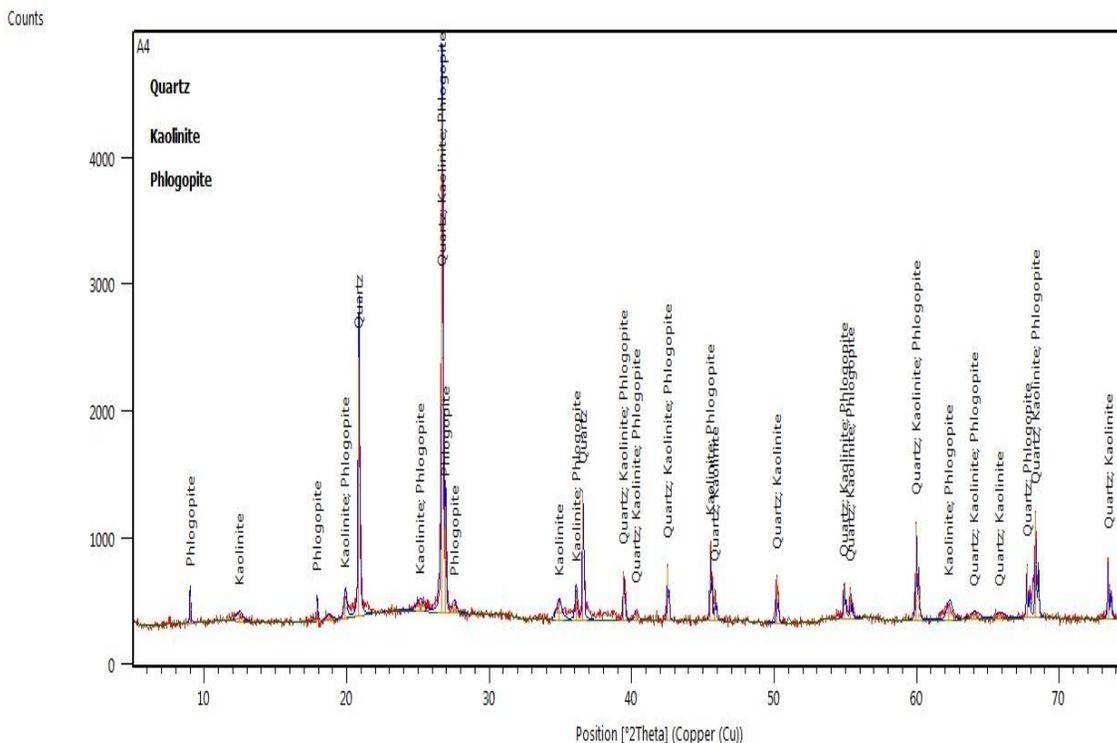


Figure 2: Results of XRD analysis of Zinc Chloride Activated Clay

Esterification Process Results

Esterification technique was used to obtain the responses and yield of Zinc Chloride Activated Catalyst (ZAC) as shown in Table 5.

Table 5: Showing Responses and Yield of ZAC

Std	Run	Factor 1A (°C)	Factor 1B (min)	Factor 1C (ml)	Factor 1D(g)	Factor 1E (mic)	Response (ml)	Yield (%)
37	1	70	30	3.75	0.25	200	31.00	32.61
22	2	70	360	2.5	0.38	200	18.50	59.78
23	3	70	30	5	0.38	200	40.00	13.04
29	4	70	195	2.5	0.38	100	20.00	56.90
26	5	90	195	3.75	0.25	200	26.50	42.39
1	6	50	30	3.75	0.38	200	30.90	32.85
32	7	70	195	5	0.38	300	36.40	20.35
46	8	70	195	3.75	0.38	200	30.00	34.78
10	9	70	360	3.75	0.38	100	28.90	37.72
34	10	90	195	3.75	0.38	100	28.50	38.58
21	11	70	30	2.5	0.38	200	21.20	53.91
35	12	50	195	3.75	0.38	300	31.80	30.42
8	13	70	195	5	0.5	200	39.00	15.22
4	14	90	360	3.75	0.38	200	26.40	42.61
2	15	90	30	3.75	0.38	200	30.60	33.48

11	16	70	30	3.75	0.38	300	30.50	33.26
31	17	70	195	2.5	0.38	300	20.40	55.36
3	18	50	360	3.75	0.38	200	30.60	33.48
24	19	70	360	5	0.38	200	35.40	23.04
16	20	90	195	5	0.38	200	36.00	21.74
44	21	70	195	3.75	0.38	200	30.40	33.91
12	22	70	360	3.75	0.38	300	27.50	39.82
36	23	90	195	3.75	0.38	300	27.50	39.82
17	24	70	195	3.75	0.25	100	30.30	34.70
18	25	70	195	3.75	0.5	100	30.80	33.62
45	26	70	195	3.75	0.38	200	30.40	33.91
33	27	50	195	3.75	0.38	100	31.50	32.11
25	28	50	195	3.75	0.25	200	32.10	30.22
20	29	70	195	3.75	0.5	300	30.50	33.26
27	30	50	195	3.75	0.5	200	33.00	28.26
30	31	70	195	5	0.38	100	38.50	17.03
42	32	70	195	3.75	0.38	200	30.40	33.91
41	33	70	195	3.75	0.38	200	29.00	36.96
39	34	70	30	3.75	0.5	200	30.50	33.70
6	35	70	195	5	0.25	200	38.50	16.30
43	36	70	195	3.75	0.38	200	30.30	34.13
38	37	70	360	3.75	0.25	200	29.00	36.96
19	38	70	195	3.75	0.25	300	30.50	33.26
40	39	70	360	3.75	0.5	200	28.80	37.39
7	40	70	195	2.5	0.5	200	20.50	55.43
28	41	90	195	3.75	0.5	200	28.00	39.13
14	42	90	195	2.5	0.38	200	18.90	58.91
5	43	70	195	2.5	0.25	200	19.50	57.61
13	44	50	195	2.5	0.38	200	21.00	54.35
9	45	70	30	3.75	0.38	100	31.50	32.11
15	46	50	195	5	0.38	200	38.70	15.87

Result of ANOVA for Zinc Chloride Activated Clay (ZAC)

The result of ANOVA for Zinc Chloride Activated Clay (ZAC) is shown in table 6. The ANOVA result showed that RSM model is significant of the experimental results as indicated from the F – value of 124.44 calculated and very low probability value of $P < 0.0001$. The lack of fit F – value of 8.71 showed that it was significant and there is 23.07% chance that a Lack of Fit F – value this large could occur due to noise. The significant terms of the model was determined by F- value and P- values. The values of “Prob> F” less than 0.0500 indicate the model terms are significant while values greater than 0.100 indicate that the model terms are not significant. ANOVA involves subdividing the total variation of a set of data onto component parts. The F – value is defined as the ratio of the mean square of regression (MRR) to the error (MRe). The smaller the magnitude of the F – value, the more significant is the corresponding coefficient [31]. The regression model demonstrates that the model is highly significant as evident from the calculated F-value (207.52) and a very low probability value ($P = 0.0001$). The lack of fit F-value of 2.50 implies that it

was not significant relative to the pure error and there is a 15.67% chance that a “Lack of Fit F-value this large could occur due to noise. If P – value of lack of fit is less than 0.05, there is statistically significant lack of fit at 95% confidence level [32].

The result in Table 6 also indicate that the significant model terms A, B, C, AB and C² implies that only linear effects of temperature, process duration, excess reactants, and interactive effects of temperature and process duration, and quadratic effects of excess reactants were significant. The model accuracy was confirmed by the correlation coefficient of the regression model which is 0.9551. The correlation coefficient showed that 95.51% of the total variation in the final concentration was attributed to the experimental variables considered in this research work. The high value of the R² and the “Pred R-Squared” of 0.8236 is in good agreement with the “Adj R – Squared” of 0.9192 as reported in literature by Mohd and Rasyidah, 2010; [31].

Final equation in terms of coded factors gives:

$$\text{Yield} = + 34.60 + 3.69A + 2.86B - 19.35C - 0.50D + 0.17E + 2.13AB + 0.33AC - 0.32 AD + 0.73AE + 1.03BC - 0.17BD + 0.24BE + 0.27CD + 1.21CE + 0.27DE + 0.62A^2 + 0.75B^2 + 2.34C^2 - 0.56D^2 + 0.13E^2. \quad (4)$$

The coefficient with one factor represent the effect of the particular factor, while the coefficients with two factors and those with second order terms represent the interaction between two factors and quadratic effect respectively (Mohd and Rasyidah 2010).

Final model equation after eliminating the insignificant terms in terms of coded variables:

$$\text{Yield} = + 34.60 + 3.69A + 2.86B - 19.35C + 2.13AB + 2.34C^2 \quad (5)$$

Table 6: ANOVA Table for Zinc Chloride Activated Clay (ZAC)

Source	Sum of Squares	df	Mean Square	F - Value	P – Value Prob> F
Model	6443.58	20	322.18	124.44	<0.0001 significant
A - Temperature	218.30	1	218.30	84.32	<0.0001
B – Process duration	131.33	1	131.33	50.72	<0.0001
C – Excess reactant	5993.08	1	5993.08	2314.73	<0.0001
D – Effect of Catalyst	4.04	1	4.04	1.56	0.2232
E – Particle size	0.48	1	0.48	0.19	0.6695
AB	18.06	1	18.06	6.98	0.0140
AC	0.43	1	0.43	0.17	0.6874
AD	0.42	1	0.42	0.16	0.6897
AE	2.15	1	2.15	0.83	0.3713
BC	4.26	1	4.26	1.65	0.2111
BD	0.11	1	0.11	0.042	0.8392
BE	0.23	1	0.23	0.087	0.7703
CD	0.30	1	0.30	0.12	0.7353
CE	5.90	1	5.90	2.28	0.1435
DE	0.29	1	0.29	0.11	0.7400
A ²	3.38	1	3.38	1.31	0.2639
B ²	4.92	1	4.92	1.90	0.1803
C ²	47.82	1	47.82	18.47	0.0002
D ²	2.71	1	2.71	1.05	0.3159
E ²	0.15	1	0.15	0.058	0.8121
Residual	64.73	25	2.59		
Lack of fit	57.48	20	2.87	1.98	0.2307 not significant

Pure Error	7.25	5	1.45		
Cor Total	6508.31	45			

Residual Plots for ZAC

The regression model developed was further assessed using residual plots. Residual is the difference between the experimental value and value predicted by the model. Some of the residual plots used were: plot of residual vs. predicted values which tests the assumption of constant variance of the experimental data, plot of residuals vs. run which checks for lurking variables that may have influenced the response during the experiment, normal plot of residuals which indicates whether the residuals follow a normal distribution, and plot of predicted vs. Actual response values which helps to detect a value, group of values that the model does not easily predict.

The residual plots for ZAC are shown in Figure 3 – 4. The trends of the residual plots indicate that the model can be considered as a good fit and that the regression equations follow the experimental results with a good accuracy. The plots indicate values that are not easily predicted by the model. The plot of residuals against run checks for lurking variables that may have influenced the response during the experiment. The normal plot of residuals indicates whether the residuals follow a normal distribution, and the plot of predicted against actual response values helps to detect a value, group of values that are not easily predicted by the model.

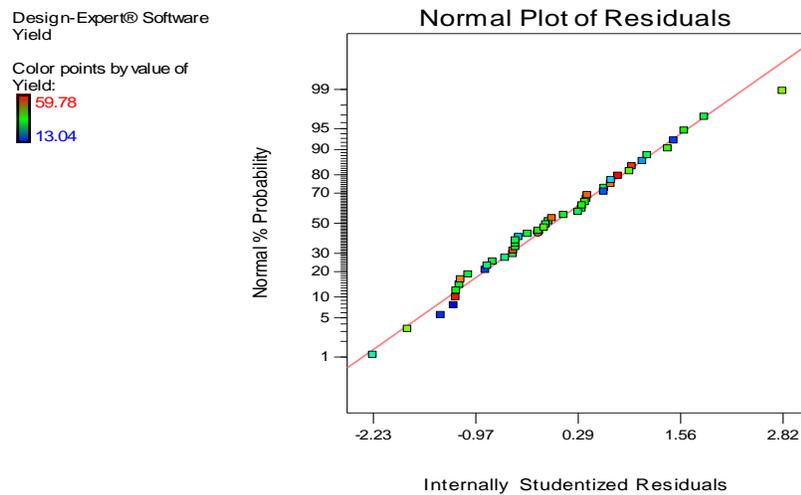


Figure 3: Normal plot of residual for ZAC

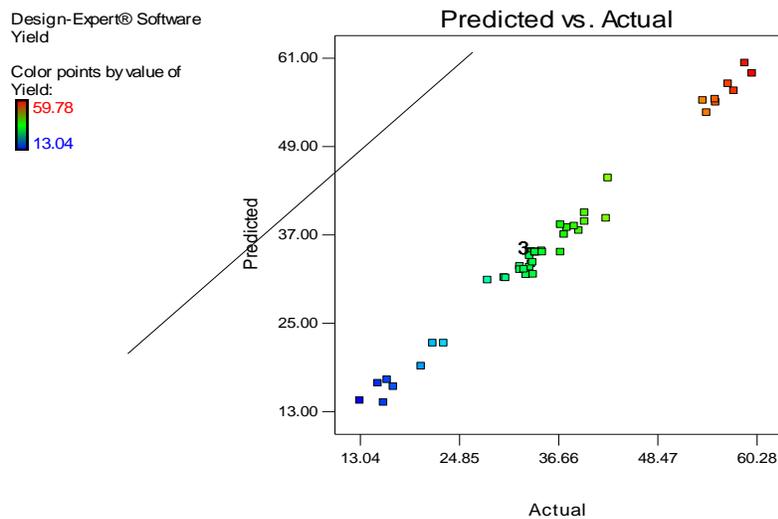


Figure 4: Plot of predicted verse actual for ZAC

Contour Plots of ZAC

The contour plots of ZAC were depicted in Figures 5 to 14. The circular nature of the contour plots indicates that the interactive effects between the variables are not significant, and the optimum values of the test process variables cannot be easily

determined[33,31]. The non-circular nature of the contour plots reveals that there is an interaction between the process variables studied, and the optimum value of the process variables can be easily obtained.

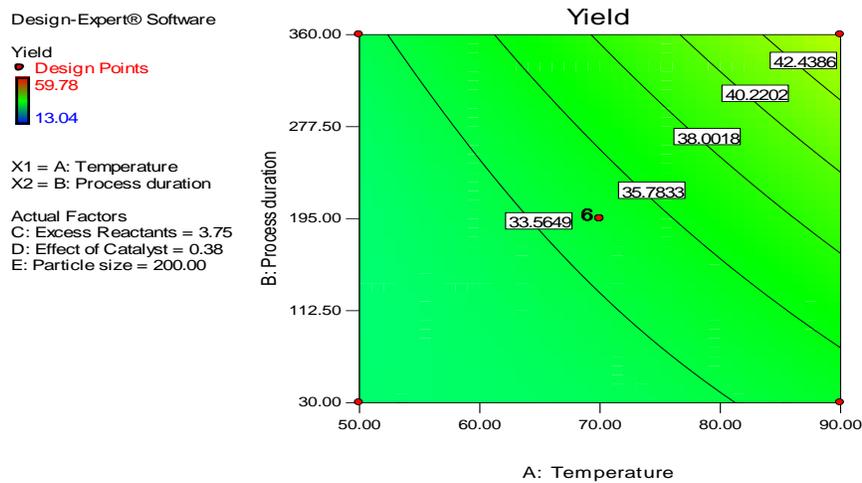


Figure 5: The contour plots for process duration against temperature and yield of ZAC

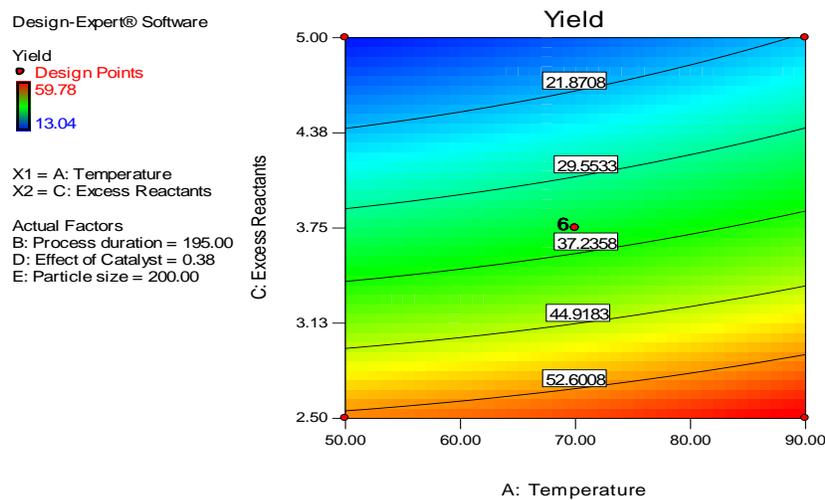


Figure 6: The contour plots for excess reactants against temperature and yield of ZAC

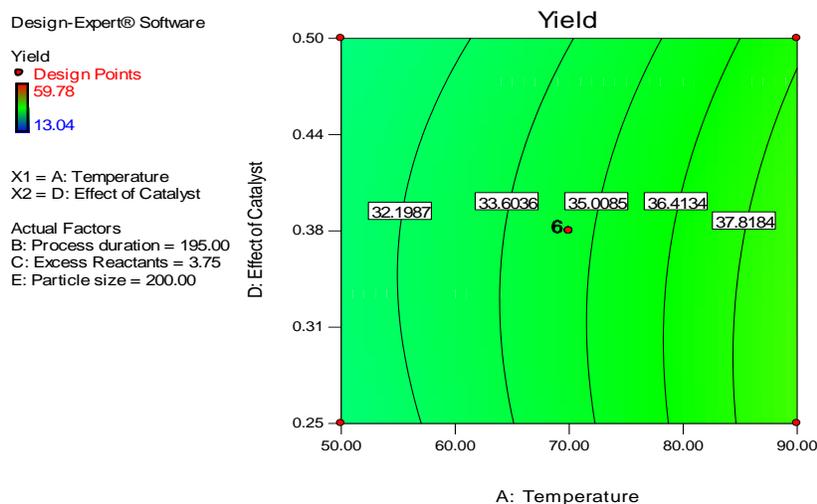


Figure 7: The contour plots for effect of catalyst against temperature and yield of ZAC

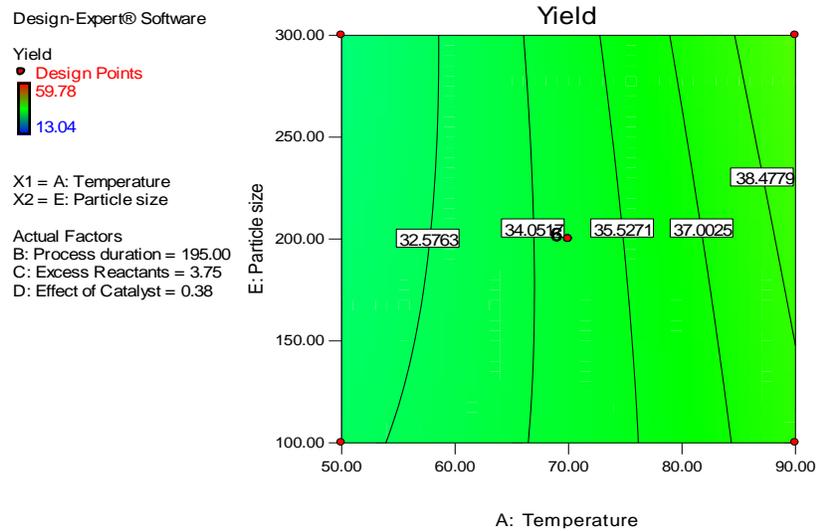


Figure 8: The contour plots for particle size against temperature and yield of ZAC

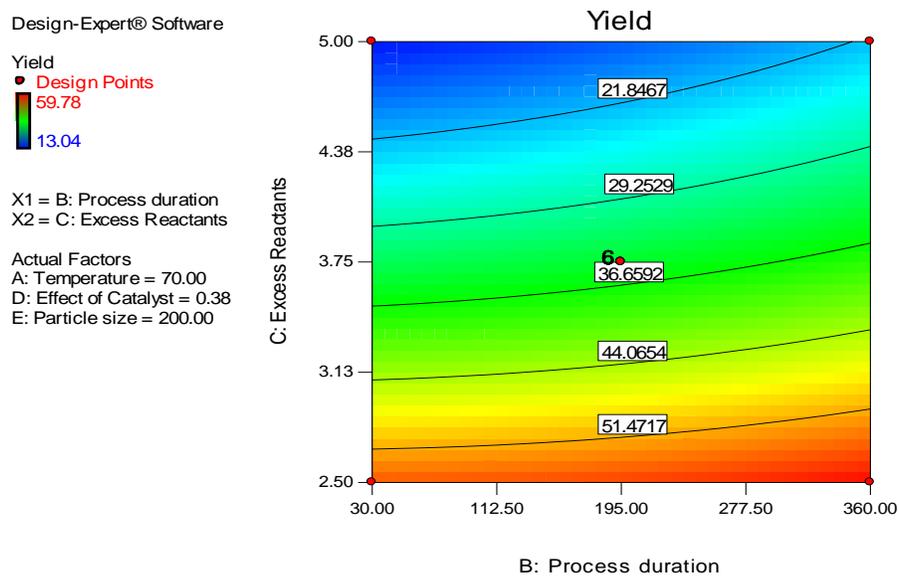


Figure 9: The contour plots for excess reactants against process duration and yield of ZAC

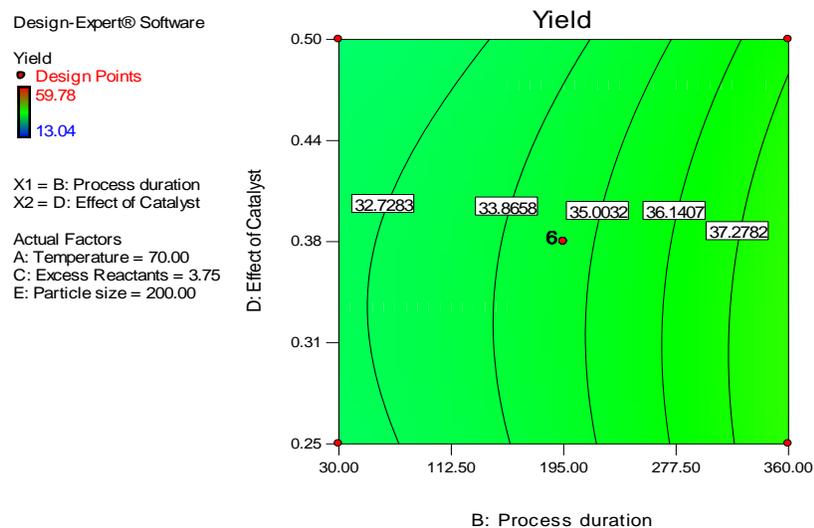


Figure 10: The contour plots for effect of catalyst against process duration and yield of ZAC

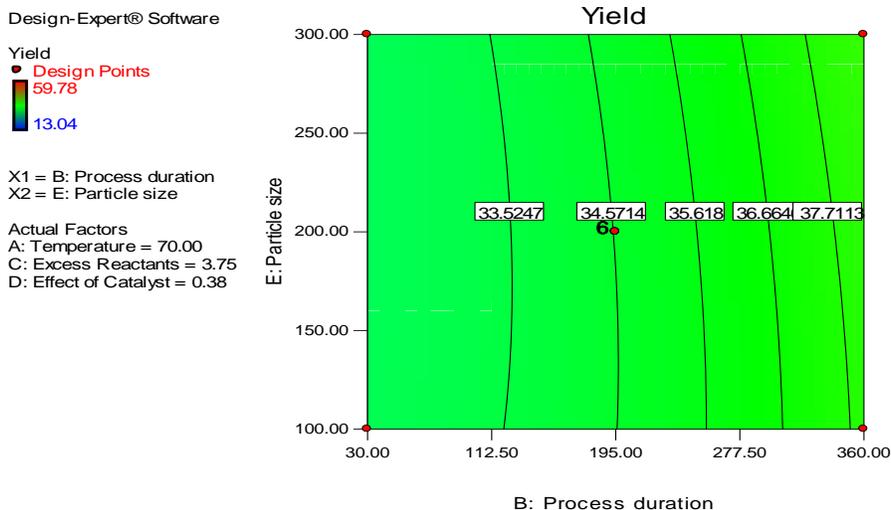


Figure 11: The contour plots for particle size against process duration and yield of ZAC

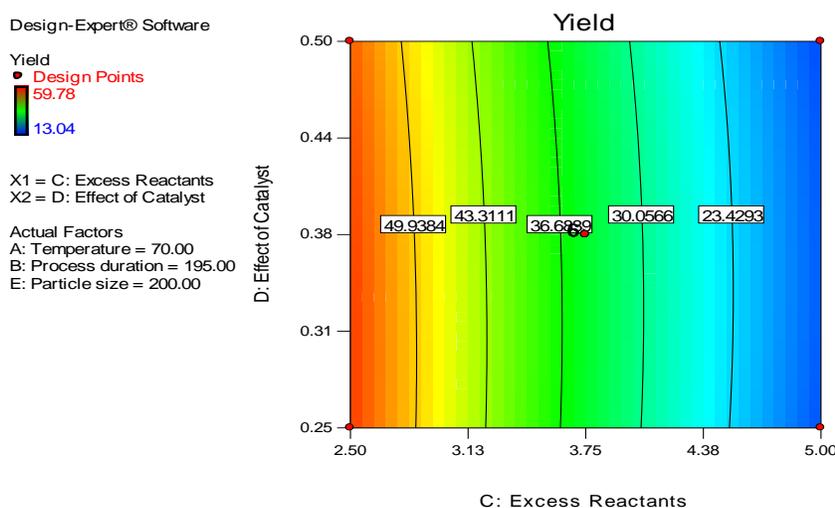


Figure 12: The contour plots for effect of catalyst against excess reactants and yield of ZAC

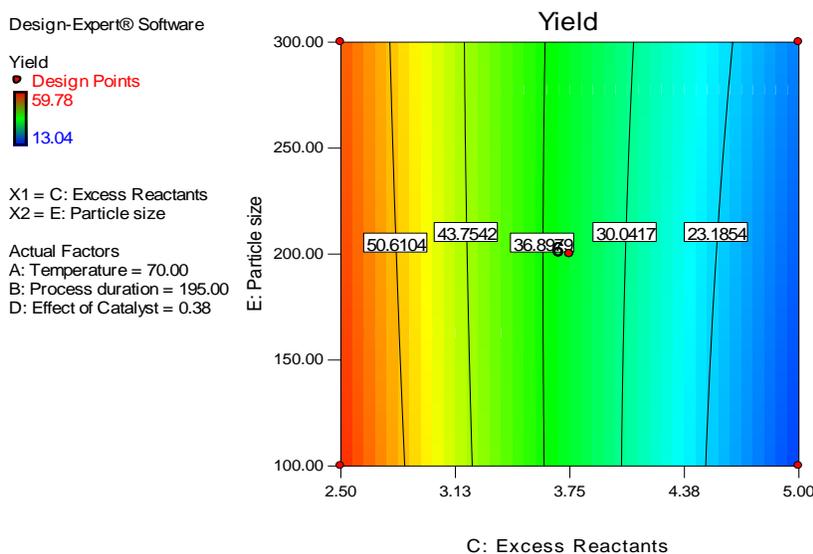


Figure 13: The contour plots for particle size against excess reactants and yield of ZAC

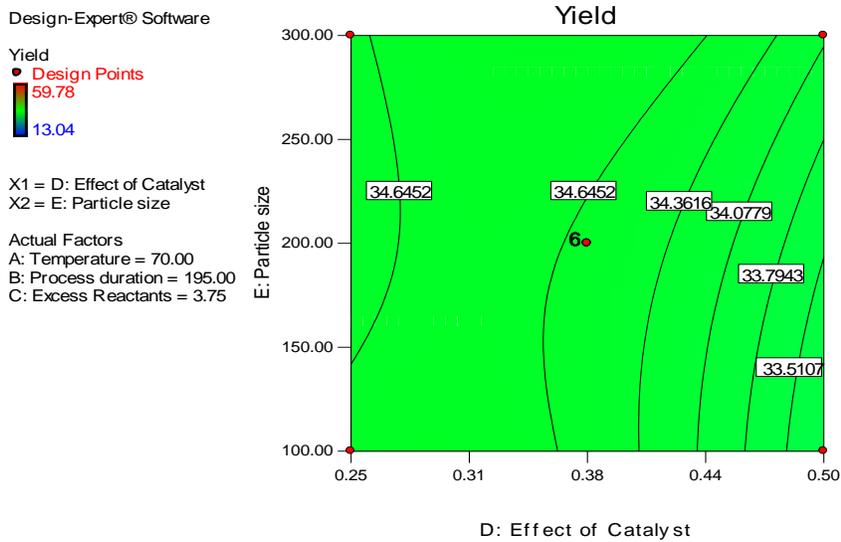


Figure 14: The contour plots for particle size against the effect of catalyst and yield of ZAC

3-D Plot of ZAC

The 3 – Dimensional plots of the response surface model for ZAC are shown in figures 15 to 24. The results showed that the optimum value of the conversion was 42 for the process variables studied, which is similar to the results obtained by [34,23,24,35]. The excess reactants increase with process duration as the yield also increases. The response surface plots showed clear peaks, implying that the maximum values of the response were attributed to the factors in the design space. The three-dimensional surfaces provide useful information about the behaviour of the system within the experiment design, facilitating an examination of the effects of the experimental factors on the responses and contour plots between the factors [33,36,37]. The 3D plots were generated by continually varying any two variables while maintaining all other input variables constant at their null point. The 3D curves were observed to have an elliptical nature with any two concerned variables. This denotes that the quadratic model chosen was appropriate, with significant correlation between the two variables [38,39].

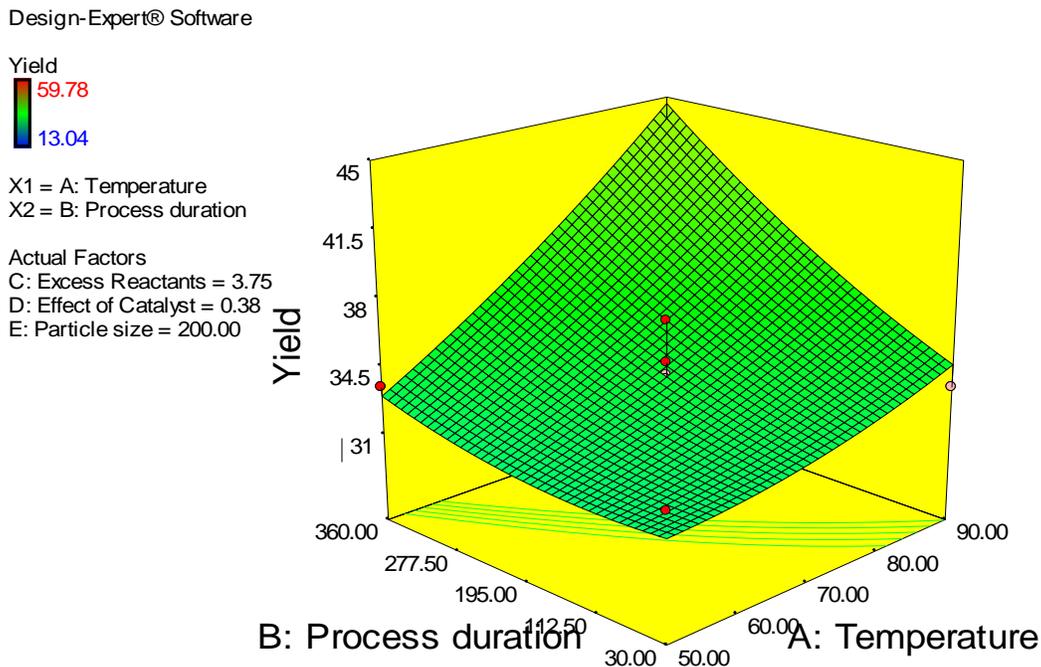


Figure 15: The 3 - D Plot for process duration against temperature and yield of ZAC

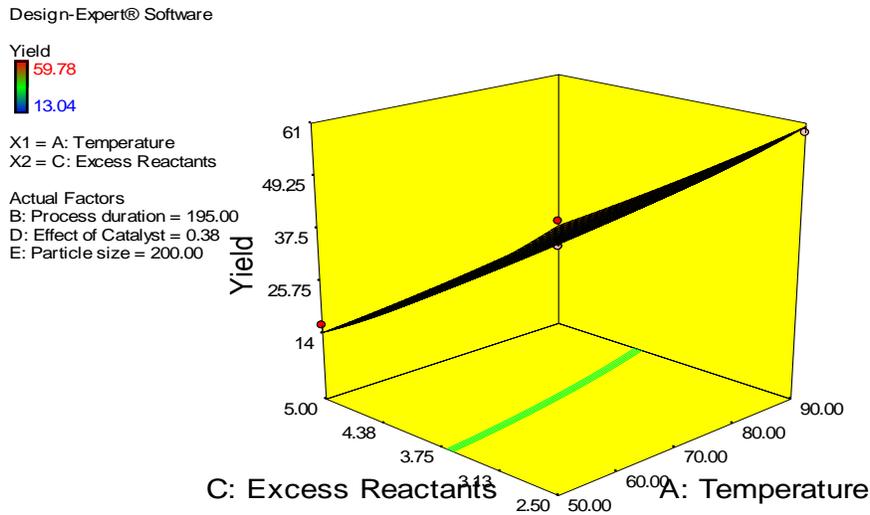


Figure 16:The 3 - D Plot for excess reactants against temperature and yield of ZAC

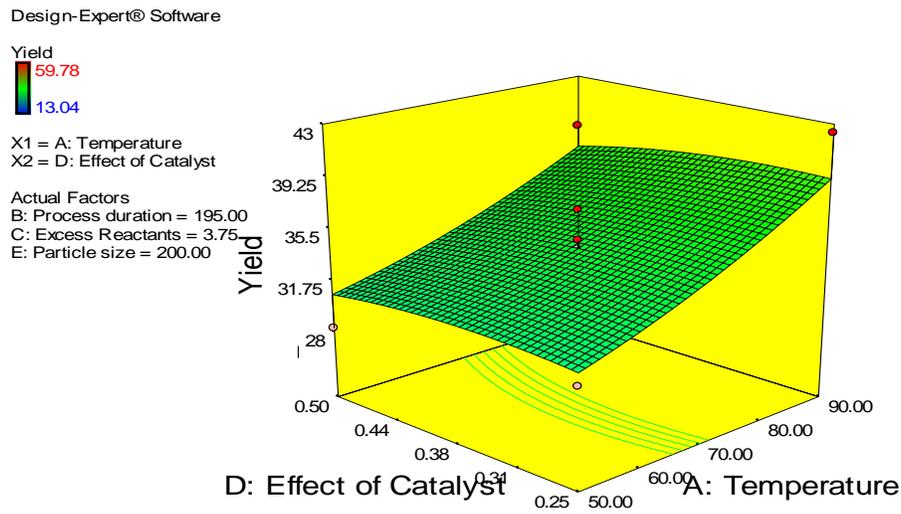


Figure 17:The 3 - D Plot for effect of catalyst against temperature and yield of ZAC

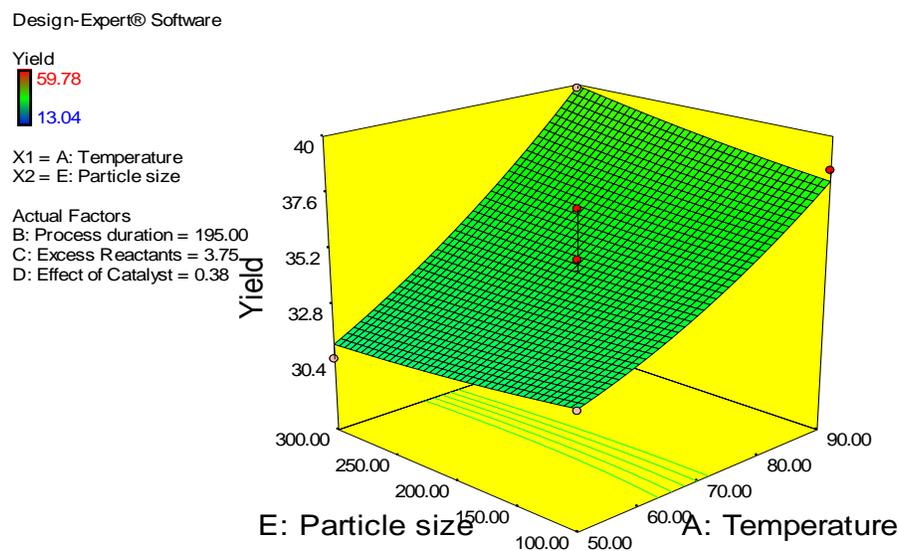


Figure 18:The 3 - D Plot for particle size against temperature and yield of ZAC

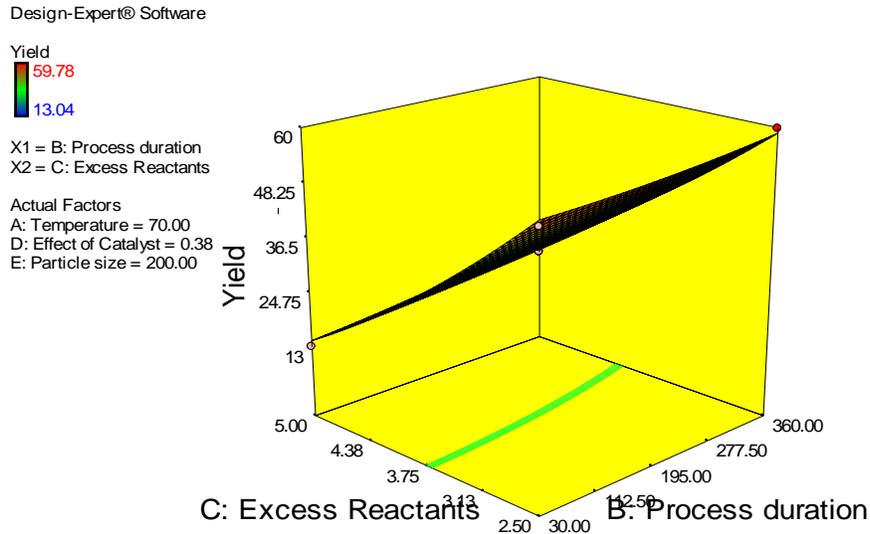


Figure 19: The 3 - D Plot for excess reactants against process duration and yield of ZAC

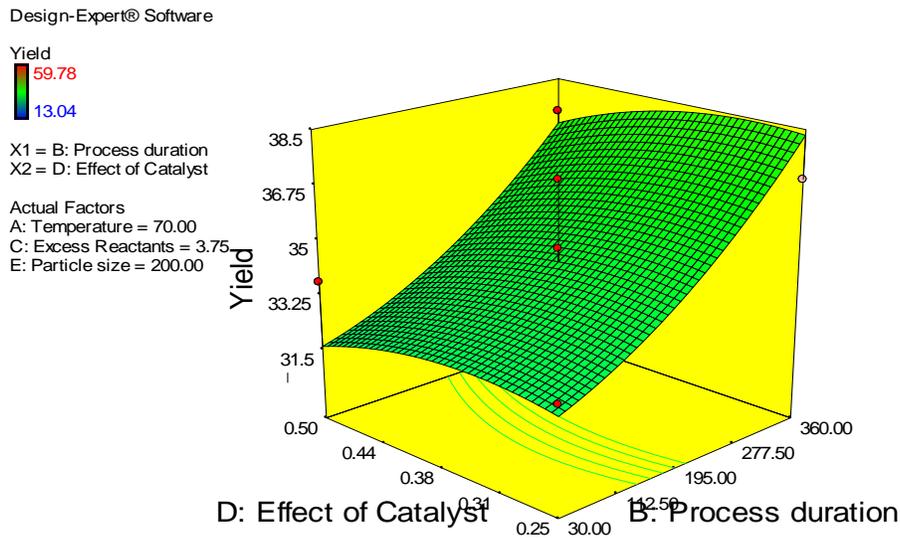


Figure 20: The 3 - D Plot for effect of catalyst against process duration and yield of ZAC

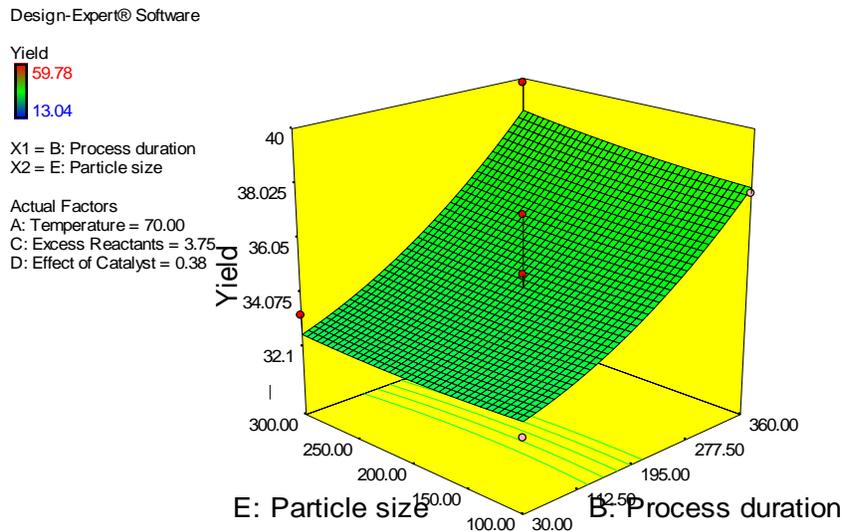


Figure 21: The 3 - D Plot for particle size against process duration and yield of ZAC

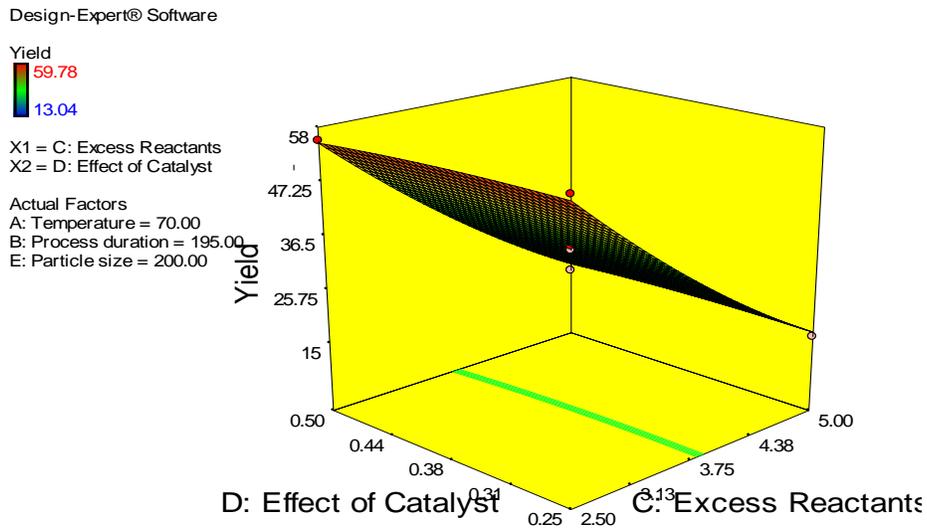


Figure 22:The 3 - D Plotfor effect of catalyst against excess reactants and yield of ZAC

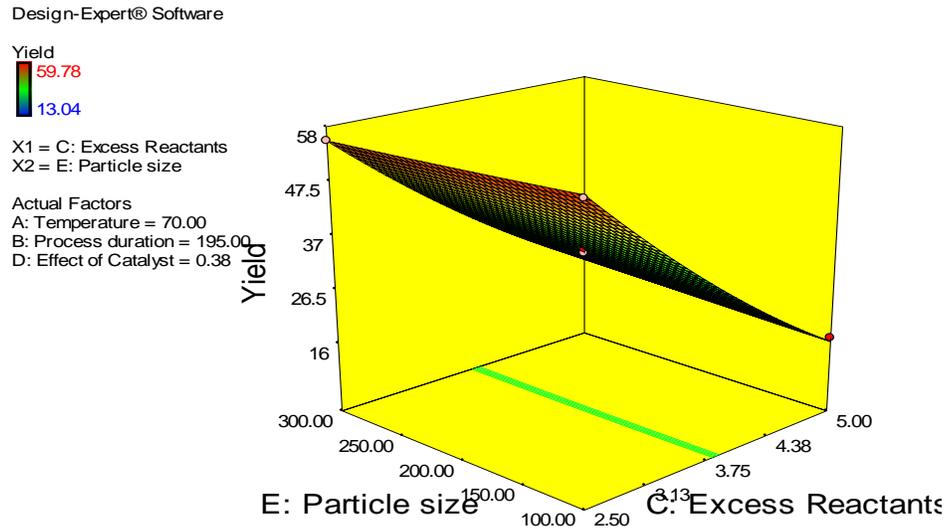


Figure 23:The 3 - D Plotfor particle size against excess reactants and yield of ZAC

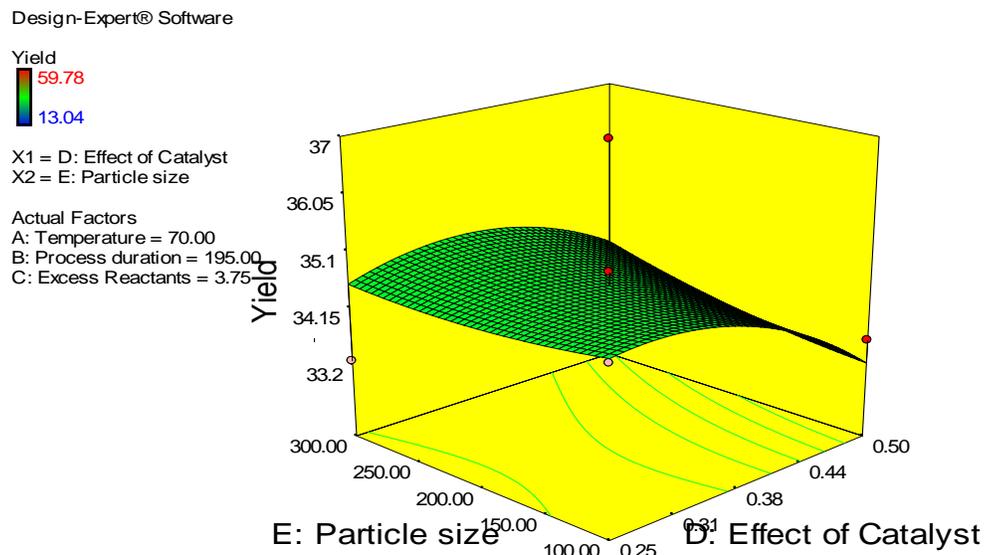


Figure 24:The 3 - D Plotfor particle size against effect of catalystand yield of ZAC

Process Optimization

In the process optimization for ZAC at table 7, desirability function was used to obtain the optimum value. The time and temperature were set at minimum while the catalyst weight, particle size and excess reactant were set in range. The conversion yield was set at maximum. The optimum process conditions for the variables were 360 min, 90°C, 4.63ml, 0.50g, and 298.67 microns for time, temperature, excess reactant, Catalyst weight and particle size respectively. The predicted conversion yield was 34.1841. The optimization was validated at those experimental conditions and conversion yield of 48.40 was obtained.

Table 7: Validation of Optimization Results

Catalysts	Model Desirability	Temp (°C)	Time (min)	Excess Reactant (ml)	Catalyst Weight (g)	Particle Size (microns)	Yield (ml)	% Conversion	% Error
ZAC	34.1841	90	360	4.63	0.50	298.67	23.00	48.40	23.00

The summary of the model validation for the catalyst produced (ZAC) is shown in Table 7. The result indicates that Ngbo ZAC is a good catalyst produced when compared to other catalysts produced from Ngbo as a result of its lower percentage error and its pH being alkaline.

V. Conclusions

The study presented the optimum conditions for the esterification reaction of acetic acid and ethanol using Zinc Chloride activated Ngbo clay catalyst. The optimum conditions for esterification reaction for the process conditions of temperature, duration, amount of reactant, catalyst weight and particle size were determined using Response Surface Methodology (RSM) approach. The optimum process conditions for the variables studied including time, temperature, excess reactant, catalyst weight and particle size were 360 min, 90 °C, 4.63ml, 0.50g, and 298.67 microns, respectively. The maximum predicted esterification yield was 34.1841. The XRF analysis revealed that the clay was primarily composed of SiO₂ and aluminium, while the XRD analysis indicated quartz as the major component. The predicted and experimental values from the model showed less than 5% difference thereby making the Box-Behnken design approach an efficient, effective and reliable method for the esterification of acetic acid and ethanol using Ngbo Zinc Chloride activated clay catalyst.

Competing Interests

Authors have declared that no competing interests exist.

References

- Nwabanne, Joseph T., Onu, Chijioko E. and Nwankwoukwu, Okwudili C. (2018) Equilibrium, Kinetics and Thermodynamics of the Bleaching of Palm Oil Using Activated Nando Clay. *Journal of Engineering Research and Reports* 1(3): 1-13. DOI: 10.9734/JERR/2018/42699
- Ajemba R.O, Onukwuli O.D (2012) Process optimization of sulphuric acid leaching of alumina from Nteje clay using central composite rotatable design. *International Journal of Multidisciplinary Sciences and Engineering*. 2012;3(5):1–6.
- Onu, C. E. and Nwabanne, J. T. (2014) “Application of Response Surface Methodology in Malachite green adsorption using Nteje clay”. *Open Journal of Chemical Engineering and Science*. 1 (2) 19 – 33.
- Nwobasi Veronica Nnenna, Igbokwe Philomena K., and Onu Chijioko Elijah (2020) Removal of Methylene Blue Dye from Aqueous Solution Using Modified Ngbo Clay. *Journal of Materials Science Research and Reviews*, 5(2): 33-46. May 2020
- Elijah, C. O. and Nwabanne, J. T. (2014). “Adsorption kinetics for Malachite green removal from aqueous solution using Nteje clay”. *Journal of Environment and Human*. 1 (2) 133 – 150. doi: :10.15764/EH.2014.02015
- Ravendra Reddy, C; Lyengar, P; Nagendrapa, G; Jai Prakash, B.S (2005).” Esterification of dicarboxylic acids to diesters over Mn⁺-montmorillonite clay catalysts” *Catalyst Letter*, 101, 87 – 91.
- Chen C-C, Hayes KF (1999) X-ray absorption spectroscopy investigation of aqueous Co(II) and Sr(II) sorption at clay-water interfaces. *GeochimCosmochimActa* 63:3205–3215
- Yadav, G.D; Thagathar, M.B(2002). “Esterification of maleic acid with ethanol over cation-exchange resin catalyst” *React. Funct.Polym*, 52, 99 – 110.
- Zang, Y; Ma, L; Yang, J (2004). Kinetics of esterification of lactic acid with ethanol catalysed by cation-exchange resins” *React. Funct.Polym*, 61, 101 – 114.
- Kirumakki S.R.; Nagaraju N; Chary, K.V.R (2006). “Esterification of alcohols with acetic acid over zeolites H β , HY and HZSM5” *Applied Catalysis A: General*, 299, 185 – 192.
- Kirumakki S.R.; Nagaraju N; Narayanan, S.A(2004).” Comparative esterification of benzyl alcohol with acetic acid over zeolites H β , HY and HZSM5” *Applied Catalysis A: General*, 273, 1 – 9.
- Wu, K; and Chen, Y (2004).“An efficient two-phase reaction of ethyl acetate production in modified ZSM- 5 zeolites” *Applied Catalysis A: General*, 257, 33 – 42.
- Chu, W. Yang, X; Ye, X; Wu, Y(1996). “Vapour phase esterification catalysed by immobilized dodecatungstosilicic acid (SiW₁₂) on activated carbon” *Applied Catalysis A: General*, 145, 125 – 140.

14. Sepulvega, J.H; Yori, J.C; Vera, C.R (2005). "Repeated use of supported $H_3PW_{12}O_{40}$ catalysts in the liquid phase esterification of acetic acid with butanol" *Applied Catalysis A: General*, 288, 18 – 24.
15. Jermy, B.R;Pandurangan,A (2005)." Catalytic application of Al-MCM-41 in the esterification of acetic acid with various alcohol". *Applied Catalysis A: General*, 288, 25 – 33.
16. Kirumakki S.R.; Nagaraju N; Chary, K.V.R; Narayanan, S (2003). "Kinetics of esterification of aromatic carboxylic acids over zeolites H β and HZSM5 using dimethyl carbonate" *Applied Catalysis A: General*, 248, 161 – 167.
17. Ezedinma Henry C., NwabanneJosph T., E. OnuChijioke E., and Nwajinka Charles O. (2021) Optimum Process Parameters and Thermal Properties of Moisture Content Reduction in Water Yam Drying. *Asian Journal of Chemical Sciences*, 9(4): 44-54, April 2021. DOI: <https://doi.org/10.9734/AJOCS/2021/v9i419080>
18. OnyekweluJeoma U., NwabanneJosph T., and OnuChijioke E., (2021) Characterization and Optimization of Biodiesel Produced from Palm Oil Using Acidified Clay Heterogeneous Catalyst. *Asian Journal of Applied Chemistry Research* 8(3): 9-23, May 2021. DOI: <https://doi.org/10.9734/AJACR/2021/v8i330192>
19. Onu, C. E., Igbokwe, P. K., Nwabanne, J. T., &Ohale, P. E. (2021). ANFIS, ANN, and RSM modeling of moisture content reduction of cocoyam slices. *Journal of Food Processing and Preservation*, 00, e16032. <https://doi.org/10.1111/jfpp.16032>
20. Iheanacho Chamberlain Ositadinma, Nwabanne Joseph Tagbo and OnuChijioke Elijah (2019) Optimum Process Parameters for Activated Carbon Production from Rice Husk for Phenol Adsorption. *Current Journal of Applied Science and Technology*, 36(6): 1-11. DOI: 10.9734/CJAST/2019/v36i630264
21. Igbokwe P. K, Nwokolo S. O, and Ogbuagu J. O, (2005).Catalytic esterification of stearic acid using a local kaolinitic clay mineral.NJERD, 4, 1.
22. Igbokwe P. K and Olebunne F. L,(2011). On the catalytic esterification of acetic acid with ethanol, using Nigerian montmorillonite clay: effect of reaction variables on catalyst efficiency. *Journal of the University of Chemical Technology and Metallurgy*, 46, 6, 389-394.
23. Igbokwe P. K, Ugonabo V. I, Obarandiku E, Ochili A, (2008) "Characterization and use of catalyst produced from local clay resources" *Journal of Applied Sciences (JAS)*, 2, 2.
24. Igbokwe, P.K., Olebunne, F.L., and Nwakaudu, M.S (2011)., Effect of Activation Parameters on Conversion in Clay – Catalysed Esterification of Acetic Acid, *International Journal of Basic and Applied Sciences*, 11.,5, 1 – 8,
25. Murat, M., A. Amokrane, J.P. Bastide, and L. Montanaro,(1992). "Synthesis of zeolites from thermally activated kaolinite. Some observations on nucleation and growth".*Clay Minerals*, 27, 1, 119.
26. Akolekar, D., A. Chaffee, and R.F. Howe (1997), "The transformation of kaolin to low-silica X zeolite". *Zeolites*, 19, 5–6, 359–365.
27. Demortier A., Golbeltz N., Letlieur J.P., Duhayon C.(1999). Infrared evidence for the formation of an Intermediate compound, during the synthesis of Zeolite Na – A from metakaolin. *International Journal of Inorganic materials*. Volume 1, issue 2, August 1999, pages 129 – 134
28. Tracy, M.M.J. and J.B. Higgins,(2001) "Collection of simulated XRD powder patterns of Zeolites" Fourth revised edition ed. 2001, Amsterdam Elsevier 379.
29. .Evamako O. Yusuf, Efeovbokhan V.E, and Babalola R. (2001). Development and characterization of zeolite – A from Elefun kaolin. *Journal of physics conference, series* 1378 – 032016.
30. Ramirez J.H, Maidonaldo – Hedar F.J, Ferez A.F, Moremo C., Costa C.A. Madeira L.M. (2007). Azo-dye orange II degradation by heterogeneous Fenton-like reaction using carbón– Fe catalysts. *Applied catalysis B: Environmental*. Volume 75, issue 3 – 4,26 September 2007, pages 312 – 323.
31. Ejikeme, M.E., P.C.N. Ejikeme, and B.N. Abalu.(2013). "RSM Optimization Process for Uptake of Water from Ethanol Water Solution Using Oxidized Starch". *Pacific Journal of Science and Technology*. 14, 2 :319-329.
32. Azargohar, R, and A.K. Dalai(2005) "Production of Activated Carbon from Luscar Char: Experimental and Modeling Studies". *MicroporMesopor. Mater.*85:219 – 225.
33. Anupam, K., S. Dutta, C. Bhattacharjee, and S. Datta (2011) "Adsorption Removal of Chromium (VI) from Aqueous Solution over Powdered Activated Carbon: Optimization through Response Surface Methodology. *Jornal of Hazard.Mater.*173:135 – 143.
34. Igbokwe P. K, Ugonabo V. I, Iwegbu N. A, Akachukwu P. C, Olisa C. J, (2008). Kinetics of the catalytic esterification of propanol with ethanoic acid using catalyst obtained from Nigerian clays. *Journal of the University of Chemical Technology and Metallurgy*, 345 – 348.
35. Olebunne F. L; Igbokwe P. K; Onyelucheya O. E; Osoka E. C and Ekeke I. C. (2011)."Mechanistic modeling of clay-catalysed liquid-phase esterification of acetic acid".*Journal of Emerging Trends in Engineering and Applied Sciences*, 2, 4: 631- 635.
36. Panesar, P.S. (2008)."Application of Response Surface Methodology in the Permeabilitation of Yeast Cells for Lactose Hydrolysis".*Biochem. Eng. J.* 39:91 – 96.
37. Ahmad, A.A. and B.H. Hameed(2010) "Effect of Preparation Conditions of Activated Carbon from Bamboo Waste for Real Textile Waste Water",*Journal of Hazard Mater.*173:487 – 493.
38. OnuChijioke Elijah, Igbokwe P.K, Nwabanne J.T, Nwanjinka O.C, Ohale P.E. Evaluation of Optimization techniques in predicting optimum moisture content reduction in drying potatoe slices. *Artificial intelligence in Agriculture*, 2020;4:39-47.

39. Available: <http://doi.org/10.1016/j.aia.2020.04.001>
40. Onu C.E, Nwabanne JT, Ohale P.E, Asadu CO. Comparative analysis of RSM, ANN and ANFIS and the mechanistic modelling in eriochrome black-T dye adsorption using modified clay. South African Journal of Chemical Engineering, 2021:36:24-42.
41. Available: <https://doi.org/10.1016/j.sajce.2020.12.003>.